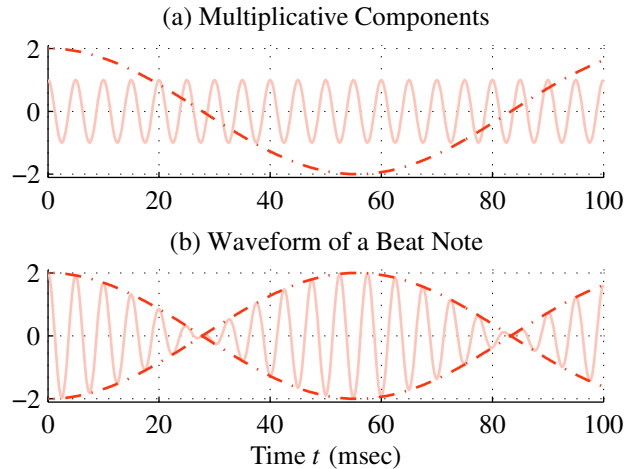


### Example 3-4: Decreasing $f_{\Delta}$

If  $f_{\Delta}$  is decreased to 9 Hz, we see in Fig. 3-4(a,b) that the envelope of the 200 Hz tone changes much more slowly. The time interval between nulls of the envelope is  $\frac{1}{2}(1/f_{\Delta})$ , so the more closely spaced the frequencies of the sinusoids



**Figure 3-4:** Beat note with  $f_c = 200$  Hz and  $f_{\Delta} = 9$  Hz. Nulls are now  $\frac{1}{2}(1/f_{\Delta}) = 55.6$  msec. apart.

in (3.10), the slower the envelope variation. These figures are simplified somewhat by using cosines for both terms in (3.10), but other phase relationships would give similar patterns. Finally, remember that the spectrum for  $x(t)$  in Fig. 3-3 contains frequency components at  $\pm 220$  Hz and  $\pm 180$  Hz, while the spectrum for Fig. 3-4 has frequencies  $\pm 209$  Hz and  $\pm 191$  Hz.