



PROBLEM:

A *unit impulse sequence* is defined as

$$\delta[n] = \begin{cases} 1 & n = 0 \\ 0 & n \neq 0 \end{cases}$$

Suppose that a LTI system has system function equal to

$$H(z) = 1 + z^{-1} - z^{-3} + 2z^{-4} - 2z^{-5}$$

- Determine the difference equation that relates the output $y[n]$ of the system to the input $x[n]$.
- Determine and plot the *impulse response*: i.e., the output sequence $y[n]$ when the input is $x[n] = \delta[n]$.
How is the output due to an impulse related to $H(z)$?



$$(a) H(z) = 1 + z^{-1} - z^{-3} + 2z^{-4} - 2z^{-5}$$

By comparison to FIR Filter's $H(z)$

$$H(z) = \sum_{k=0}^{L-1} b_k z^{-k}$$

We can read off the b_k from $H(z)$ by taking the coeffs of different powers of z^{-1}

$$\begin{aligned} b_0 &= 1 & b_3 &= -1 \text{ because we have } -z^{-3} \\ b_1 &= 1 & b_4 &= 2 \text{ } \leftarrow 2z^{-4} \\ b_2 &= 0 \text{ (no } z^{-2} \text{ term)} & b_5 &= -2 \text{ } \leftarrow \text{due to } -2z^{-5} \end{aligned}$$

Now we can write the difference Equation:

$$y[n] = x[n] + x[n-1] - x[n-3] + 2x[n-4] - 2x[n-5]$$

(b) The impulse response for FIR is just the filter coeffs:

n	< 0	0	1	2	3	4	5	$n > 5$
$h[n]$	0	1	1	0	-1	2	-2	0

