



PROBLEM:

Given a feedback filter defined via the recursion:

$$y[n] = 0.9 y[n - 4] + x[n - 2] \quad (\text{DIFFERENCE EQUATION}) \quad (1)$$

- (a) Find the z -transform operator representation for the system in (1).
- (b) Find the poles of the system and plot their location in the z -plane.



$$(a) \quad H(z) = \frac{z^{-2}}{1 - 0.9z^{-4}}$$

$$(b) \quad \text{Find roots of: } 1 - 0.9z^{-4} = 0$$

$$\Rightarrow z^4 = 0.9e^{j2\pi k}$$

$$\text{POLES} = \left\{ \sqrt[4]{0.9}e^{j\pi/2}, \sqrt[4]{0.9}e^{j\pi}, \sqrt[4]{0.9}e^{j3\pi/2}, \sqrt[4]{0.9} \right\}$$

↑ value = 0.974

