



PROBLEM:

For each of the difference equations below, determine the poles and zeros of the corresponding system function, $H(z)$. Plot the poles (**X**) and zeros (**O**) in the complex z -plane.

$$\mathcal{S}_1 : \quad y[n] = 0.4y[n-1] + x[n] + x[n-1]$$

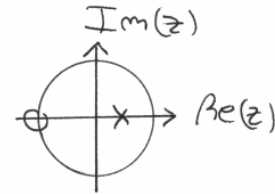
$$\mathcal{S}_3 : \quad y[n] = -0.75y[n-1] + x[n] - x[n-1]$$

$$\mathcal{S}_6 : \quad y[n] = x[n] - x[n-1] + x[n-2] - x[n-3]$$

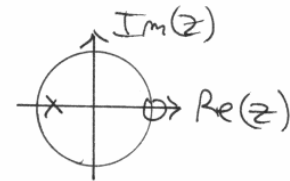
$$\mathcal{S}_7 : \quad y[n] = x[n] + \frac{1}{4}x[n-1] - \frac{3}{4}x[n-2]$$



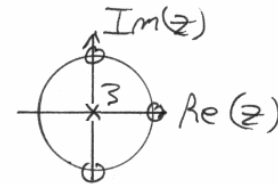
(S₁) $H_1(z) = \frac{1 + z^{-1}}{1 - 0.4z^{-1}}$ zero at $z = -1$
pole at $z = 0.4$



(S₂) $H_2(z) = \frac{1 - z^{-1}}{1 + 0.75z^{-1}}$ $z_z = 1$
 $z_p = -0.75$



(S₃) $H_3(z) = 1 - z^{-1} + z^{-2} - z^{-3}$ $z_z = 1, j, -j$
poles at $z = 0$



(S₄) $H_4(z) = 1 + \frac{1}{4}z^{-1} - \frac{3}{4}z^{-2}$ $z_z = -1, \frac{3}{4}$
poles at $z = 0$

