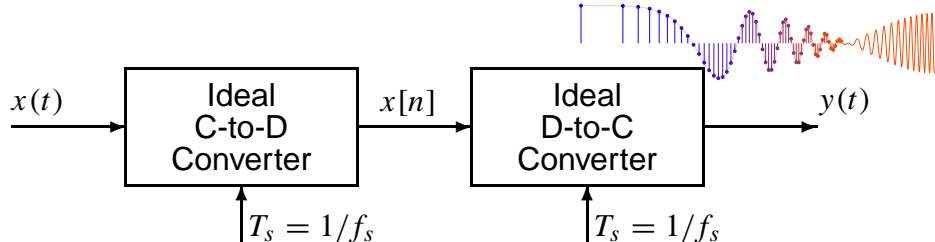


PROBLEM:



In all parts below, the sampling rates of the C/D and D/C converters are **equal**, and the input to the Ideal C/D converter is

$$x(t) = 2 \cos(2\pi(50)t + \pi/2) + \cos(2\pi(150)t).$$

(a) If the output of the ideal D-to-C Converter is

$$y(t) = x(t) = 2 \cos(2\pi(50)t + \pi/2) + \cos(2\pi(150)t),$$

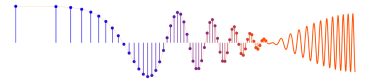
what general statement can you make about the sampling frequency f_s in this case?

(b) If the sampling rate is $f_s = 250$ samples/sec., determine the discrete-time signal $x[n]$, and give an expression for $x[n]$ as a sum of cosines. *Make sure that all frequencies in your answer are positive and less than π radians.* Plot the spectrum of this signal over the range of frequencies $-\pi \leq \hat{\omega} \leq \pi$. Make a plot for your answer, but label the frequency, amplitude and phase of each spectral component.

(c) If the output of the ideal D-to-C Converter is

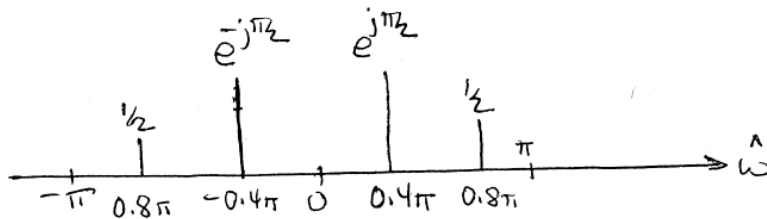
$$y(t) = 2 \cos(2\pi(50)t + \pi/2) + 1,$$

determine the value of the sampling frequency f_s . (Remember that the input $x(t)$ is as defined above.)



(a) NO ALIASING $\Rightarrow f_s > 2(150) = 300$ SAMPLES/SEC

$$\begin{aligned}
 (b) \quad x[n] &= x\left(\frac{n}{250}\right) = 2\cos\left(2\pi(50)\frac{n}{250} + \frac{\pi}{2}\right) + \cos\left(2\pi(150)\frac{n}{250}\right) \\
 &= 2\cos\left(0.4\pi n + \frac{\pi}{2}\right) + \cos(1.2\pi n) \\
 &= 2\cos\left(0.4\pi n + \frac{\pi}{2}\right) + \cos(0.8\pi n)
 \end{aligned}$$



(c) SINCE THE 50 HZ TERM IS UNCHANGED, THEN WE KNOW $f_s > 2(50) = 100$ HZ.

HOWEVER, THE 150 HZ SINUSOID ALIASES TO 0 HZ.

$$\Rightarrow f_s = 150 \text{ SAMPLES/SEC.}$$

WHY? FOR $f_s = 150$ HZ, WE HAVE $\hat{f} = \frac{150}{150} = 1$

WHICH ALIASES TO $\hat{f} = 1 - 1 = 0$.